FOCUS ISSUE

INTRINSIC AND EXTRINSIC SIZE EFFECTS IN MATERIALS

# Grain size effect on deformation twin thickness in a nanocrystalline metal with low stacking-fault energy

Yusheng Li<sup>1</sup>, Liangjuan Dai<sup>1</sup>, Yang Cao<sup>1</sup>, Yonghao Zhao<sup>1,a)</sup>, Yuntian Zhu<sup>2</sup>

<sup>1</sup>Nano and Heterogeneous Materials Center, School of Materials Science and Engineering, Nanjing University of Science and Technology, Nanjing 210094, China

<sup>2</sup>Department of Materials Science and Engineering, North Carolina State University, Raleigh, North Carolina 27695, USA

<sup>a)</sup>Address all correspondence to this author. e-mail: yhzhao@njust.edu.cn

Received: 29 November 2018; accepted: 20 May 2019

Grain size effect on twin thickness has been rarely investigated, especially when the grain size is less than 1000 nm. In our previous work (*Mater. Sci. Eng.* A527, 3942, 2010), different severe plastic deformation techniques were used to achieve a wide range of grain sizes from about 3 µm to 70 nm in a Cu–30% Zn alloy. Transmission electron microscopy (TEM) revealed a gradual decrease in the deformation twin thickness with decreasing grain size. In the present work, high-resolution TEM was used to further identify deformation twins and measure their thickness, especially for grain sizes below 70 nm. The twin thickness was found to gradually reduce with decreasing grain size, until a critical size (20 nm), below which only stacking faults were observed. Interestingly, the relationship between twin thickness and grain size in the ultrafine/nanocrystalline regime is found similar to that in the coarse-grained regime, despite the differences in their twinning mechanisms. This work provides a large set of data for setting up a model to predict the twin thickness in ultrafine-grained and nanocrystalline face-centered cubic materials.

# Introduction

Deformation twinning in metals and alloys has been investigated extensively because it is one of the few mechanisms that can increase strength and ductility simultaneously [1, 2, 3]. It is well known that the activation of deformation twinning is affected by intrinsic physical and structural characteristics of materials [e.g., stacking-fault energy (SFE) and grain size] [4] and extrinsic deformation conditions (e.g., strain, strain rate and temperature) [5, 6]. Among these factors, the grain size effect is less explored because its significance was mainly noticed after the discovery of nanocrystalline (NC) materials. The grain size effect on deformation twinning has attracted significant attentions recently, most of which are paid to the grain size effect on twinning propensity [7, 8, 9].

As an effective dislocation barrier, it is well known that the strengthening effect of twin boundaries is considered similar to that of grain boundaries and can be evaluated by the following equation [2]:

$$\sigma_{\rm TB} = \frac{K_{\rm TB}}{\sqrt{t}} \quad , \tag{1}$$

where  $K_{\text{TB}}$  is a constant value and t is the average twin thickness. It is obvious that, when the twin thickness is larger than a critical value, the strengthening effect of twin boundaries is inversely proportional to the twin thickness [10]. Apparently, besides twinning density, twin thickness is another important microstructural feature, and increasing interests have been put on nanoscale twinned materials with unprecedented strengths [1, 11]. Twin thickness has been reported to be affected by SFE [12] and extrinsic deformation conditions such as strain rate and temperature [13]. However, the relationship between grain size and twin thickness has been rarely investigated, especially when the grain size enters into the <1000 nm regime. In 2001, Meyers et al. [14] proposed an elegant model to predict the twin embryo size (minimum twin size) as a function of twinning stress in coarse-grained materials. Meyers' model takes into account the classical Hall-Petch relationship between the global twinning stress and grain size and demonstrates that twin embryo size



decreases with the decreasing grain size in coarse-grained facecentered cubic (fcc) materials. This dislocation-based model is invalid in NC and ultrafine-grained (UFG) materials since dislocation activities are suppressed in such fine grains. Thus, it is necessary to investigate the grain size effect on twin thickness, especially for NC and UFG materials.

Although the twinning mechanisms are different in coarsegrained and NC materials, they share some similarities. For example, twins can be formed by overlapping of stacking faults [15, 16], and twinning is always stress driven [17, 18]. Therefore, it is being wondered if the twin thickness, which is theoretically governed by stress, is also affected by grain size in NC and UFG materials. In our previous work [19], high-pressure torsion (HPT) and equal-channel angular pressing (ECAP) followed by cold rolling were used to achieve a wide range of grain sizes from about 3 µm to 70 nm in a Cu-30% Zn alloy. We found that, with decreasing grain size, the average deformation twin thickness decreases gradually from 177 to 24 nm, while the density of deformation twins (the length of twin boundary in unit area) exhibits a maximum value at an ECAP + 95% rolling sample with an average grain size of 110 nm. Due to the resolution limitation of transmission electron microscopy (TEM), the twin thickness variation versus grain size below 70 nm was not investigated, and the underlying mechanism for the relationship of twin thickness versus grain size was not clarified [20]. Beyerlein et al. [20] reported that the twin thickness in Mg and Zr is independent of grain size. It is worthy to note that these conclusions were based on observations derived from optical microscopy, TEM and electron backscattered diffraction; due to the resolution limitations of these techniques, it is difficult to study the grain size effect in atomic scale, and the twinning mechanisms and twin thickness-grain size relationship need to be further clarified.

In this work, to solve the abovementioned problems, we used high-resolution TEM (HRTEM) to reexamine aspects of our previous statistical analysis in Cu–30% Zn alloy [19] that related twin thickness to grain size, especially in the grain size range below 70 nm. Cu–30% Zn alloy was selected as a model material to study this phenomenon because it has a low SFE and twinning is its dominant deformation mechanism. A large data set was created by extensive HRTEM analyses over hundreds of grains, through a wide range of grain sizes, to illustrate the relationship between twin thickness and grain sizes. The trend is found similar to what was observed/ estimated in coarse-grained materials, but below a critical grain size, only stacking faults were observed.

#### Results

Figures 1(a) and 1(b) show the bright field (BF) and dark field (DF) TEM images of the HPT-processed Cu-30% Zn alloy, respectively. The microstructure exhibits homogeneously

distributed equiaxed nanograins and ultrafine grains. Most grains contain planar structural features [see in Fig. 1(b)], which were proved to be twins and stacking faults. The relatively continuous rings of the selected area electron diffraction (SAED) pattern confirm again that there is no obvious preferential grain orientation in the NC Cu-30% Zn alloy. Figures 1(c) and 1(d) show the microstructures of the Cu-30% Zn alloy processed by ECAP + 95% rolling. Compared with that of the HPT-processed sample, the grains are obviously bigger and mostly within the UFG regime. High density of deformation twins were also found in the sample, as shown by the white arrowheads in Fig. 1(c). The SAED in Fig. 1(c) indicates the existence of texture-free equiaxed grains. Figures 1(e) and 1(f) show the microstructures of the Cu-30% Zn alloy processed by ECAP + 75% rolling. As can be seen, the grains in the sample are much bigger than that of the ECAP + 95% rolling sample. Additionally, the twin frequency appearing in an ECAP + 75% rolling sample is lower than that in an ECAP + 95% rolling sample, and only one grain containing deformation twins was identified in the ECAP + 75% rolling sample [see the white arrowhead in Fig. 1(e)].

Figure 2 gives the measured statistical grain size distributions for Cu–30% Zn alloys processed by HPT, ECAP + 95% rolling and ECAP + 75% rolling, determined from a large number of TEM images. The grain size in the HPT sample distributes from ~5 to ~160 nm with an average size of ~80 nm. ECAP + 95% rolling and ECAP + 75% rolling samples are with grain sizes distributed in the range of ~50 nm–300 nm and ~80 nm– 500 nm, respectively. The average grain size is ~160 nm for the ECAP + 95% rolling sample and ~260 nm for the ECAP + 75% rolling sample. Thus, a wide range of grain size can be derived from these three kinds of samples to study the relationship between the grain size and twin thickness.

A large number of HRTEM images reveal that grains in the size range of  $\sim 20-500$  nm contain both stacking faults and deformation twins. Figure 3(a) shows an example of a  $\sim 300$  nm grain containing deformation twins and stacking faults. The inset is an HRTEM image of the white rectangle area in Fig. 3(a), which confirms the twinning relationship. Figure 3(b) shows a BF TEM image of a  $\sim 150$  nm grain, which contains high density of twins. The thickness of the twins ranges from a few nanometers to a few tens of nanometers. Most of them passed through the whole grain, while some twins stopped in the grain interior.

Figure 3(c) shows a  $\sim$ 60 nm grain. There are many stacking faults in this grain as indicated by white arrowheads. A twin is observed at the bottom of the grain boundary (GB) denoted by M/T. The area enclosed by the white rectangle is magnified in Fig. 3(d). Grain 1 (G1) has 13.2° misorientation with grain 2 (G2). The twin was initiated at the junction between G1, G2 and the grains that are out of the low-index zone axes. Deformation





**Figure 1:** (a, b) BF and DF TEM images of the HPT sample; (c, d) BF and DF TEM images of the ECAP + 95% rolling sample; (e, f) BF and DF TEM images of the ECAP + 75% rolling sample. The diameter of the selected area diffraction aperture is (a, c) 4.0 μm and (e) 1.2 μm, respectively. White arrowheads point out some typical nanotwins.

twinning requires sufficient high stress, and a multiple boundary junction is an ideal stress concentration site as well as a dislocation source. Therefore, twinning partials have high probability to emit from a multiple boundary junction [21, 22]. The twin did not pass through the whole grain, but left an incoherent twin boundary in the grain interior, as indicated by the white dashed line. This suggests insufficient driving force for this twin to propagate through the grain [23].

Figure 4(a) shows a typical HRTEM image of a  ${\sim}40$  nm grain with many twins and staking faults. The white rectangle

3

Downloaded from https://www.cambridge.org/core. American University of Beirut, on 15 Jun 2019 at 08:36:00, subject to the Cambridge Core terms of use, available at https://www.cambridge.org/core/terms. https://doi.org/10.1557/jmr.2019.194





**Figure 2:** Measured statistical grain size distribution for Cu-30% Zn alloys processed by HPT, ECAP + 95\% rolling and ECAP + 75\% rolling, determined from a large number of TEM images.



**Figure 3:** (a) TEM image of a typical  $\sim$ 300 nm grain, the inset is the magnified image of the framed area; (b) TEM image of a typical  $\sim$ 150 nm grain; (c) HRTEM image of a typical  $\sim$ 60 nm grain; (d) magnified image of the framed area in (c) and inset of a fast Fourier-transformed pattern showing the twin relationship.

framed area in Fig. 4(a) is enlarged in Fig. 4(b), where the upper twin contains a stacking fault as indicated by a white arrowhead. The twin at the bottom of the image contains incoherent twin boundaries that stopped inside the grain. This



**Figure 4:** (a) HRTEM images of an HPT sample with a grain size of  $\sim$ 40 nm; (b) magnified image of the framed area in (a). White arrowheads point out some stacking faults and microtwins.



**Figure 5:** HRTEM images of an HPT sample with different grain sizes (a)  $\sim$  20 nm and (c)  $\sim$ 8 nm. (b, d) magnified images of framed areas in (a) and (c), respectively.

indicates that GB-mediated twinning and detwinning mechanisms are operative at this grain size [16, 24].

Figure 5(a) shows an example of an  $\sim 20$  nm grain. Figure 5(b) gives the enlarged image of white rectangle framed area in Fig. 5(a). It is clearly seen from Fig. 5(b) that there is a two-layer microtwin (extrinsic stacking fault) and two intrinsic stacking faults passing through the whole grain, as indicated by the white arrowheads. Figure 5(c) shows some typical nanograins found at the edge of an HPT sample and Fig. 5(d) shows a magnified view of an  $\sim 8$  nm grain enclosed by a white rectangle in Fig. 5(c). There are two stacking faults passing through the whole grain, as indicated by the white arrowheads. Extensive HRTEM analyses show that there are profuse stacking faults instead of deformation twins in those grains smaller than 20 nm. This suggests that twinning is no longer operative in grains smaller than 20 nm in this Cu–30% Zn alloy under the current deformation conditions.

🔳 Journal of Materials Research 🔳 www.mrs.org/jm



Figure 6 reveals the relationship between twin thickness and grain size in UFG and NC Cu-30% Zn alloy samples, derived from a large number of HRTEM images. It is noteworthy that, for a given grain size, the average twin thickness shows no big difference between the three samples; thus, Fig. 6 gives the data from the three samples without differentiation. It is clearly seen that with decreasing grain size from  $\sim$  500 to  $\sim$  20 nm, twin thickness gradually reduces to two atomic layers (a microtwin, 0.424 nm). When the grain size is below 20 nm, only one atomic layer (a stacking fault) with a thickness of 0.212 nm is found, as shown in the inset (Fig. 6). The observed relationship between twin thickness and the grain size is governed by both twinning stress and twinning mechanisms. Therefore, a preliminary attempt to explain the twin thickness and grain size relationship in UFG and NC fcc alloys can be made in section "Conclusions".

# Discussion

Dislocation-based mechanisms [15, 25] have been proposed to explain twin nucleation in coarse-grained fcc materials. Meyers et al. [14] applied the twinning nucleation mechanism [26] to predict the critical twin nucleus size above which the twin can form and grow in a stable manner. It was assumed that a twin embryo is a disk-shaped nucleus with radius  $r_c$  and thickness  $\lambda_c$ , and the relationship between  $r_c$  and  $\lambda_c$  is  $\lambda_c/r_c = \rho$ , where  $\rho$ is a constant aspect ratio. Consequently, the twin embryo size is directly related to the SFE and driving stress, as expressed by [14]

$$\lambda_{\rm c} = \frac{5\pi G}{4} \frac{\gamma_{\rm SF}}{\sigma_{\rm T}^2} \rho \quad , \qquad (2)$$

where G is the shear modulus and  $\gamma_{SF}$  is the SFE. Another variable  $\sigma_T$  is the twinning stress estimated based on the Hall-Petch relationship. Therefore, while the Hall-Petch relationship is valid,  $\sigma_T$  increases with decreasing grain size. Consequently, described by formula (2), the twin embryo size decreases with decreasing grain size in coarse-grained materials. This is similar to what has been observed in the current work in UFG and NC Cu-30% Zn alloys (Fig. 6). However, a simple adoption of formula (2) to estimate the twin embryo size and twin thickness in UFG and NC materials is inappropriate because the conventional Hall-Petch relationship and Venables' twinning model, which the formula is based on, are no longer valid in NC materials [27, 28, 29]. Notwithstanding, the similarity between the estimation by the formula and the result of our work is not a coincidence. Meyers' model considered two important factors, twinning stress ( $\sigma_T$ ) and SFE  $(\gamma_{SF})$ , which are also determinative factors for twinning in UFG and NC materials. Additionally, Meyers' model [14] assumed the stress concentration site is on the GB which is also true in NC materials [30, 31].

Once the grain sizes decrease to the UFG and NC regimes, the conventional dislocation-based twinning mechanisms cease



Figure 6: A plot of the experimental data correlating the twin thickness with the grain size in UFG and NC Cu-30% Zn alloys.

🔳 Journal of Materials Research 🔳 www.mrs.org/jmi



to operate [27]; instead, GB-mediated deformation mechanisms start to dominate [30, 32], as shown in Figs. 3–5. Twin nucleation requires a flow stress higher than both leading Shockley partial emission stress and twinning partial emission stress. As the grain size decreases, both stresses increase [3, 9, 33, 34]. Combined with the requirement of higher stress for twinning than for leading partial emission, one can envisage that below a certain critical grain size, the stress required for twinning is eventually higher than the applied flow stress; therefore, twinning will stop, but extended stacking faults can still form, as shown in Fig. 6. This is consistent with early observations in NC Ni deformed at the liquid nitrogen temperature [9].

In NC materials, SFE alone is insufficient to explain the twinning behavior; a generalized planar fault energy (GPFE) curve also plays a significant role [34]. The GPFE contains the stacking-fault energy ( $\gamma_{SF}$ ), unstable stacking-fault energy  $(\gamma_{\text{USF}})$  and unstable twin fault energy  $(\gamma_{\text{UTF}})$ . Under GBmediated twinning mechanisms, the applied stress needs to first overcome the energy barrier  $\gamma_{\text{USF}}$  to emit a leading partial to form a SF in the grain and the energy barrier  $\gamma_{\text{UTF}}$  to nucleate a two-layer twin. As the grain sizes decrease, the GB areas increase in a bulk material and the number of partial dislocation emission sites increases. However, active SF activities could delay twin formation because it relieves the local stress concentration that is needed for subsequent twin nucleation. Meanwhile, the active partial dislocation activities create single-layer SFs that are potential twin nucleation sites, which may lead to high density of twin nuclei. These nuclei will compete with each other for growth. As the grain size decreases, the twin growth competitions will limit the growth space of individual twins, which leads to smaller twin thickness. This is similar to the twin embryo growth competitions in coarse-grained low-SFE materials [12]. Moreover, detwinning activity becomes stronger with decreasing grain size due to higher flow stress to drive partial dislocation interactions with twin boundaries [9, 35, 36].

From another perspective, the space for twin embryos will be smaller when the grains get smaller; therefore, the small grain cannot contain more twin embryos, which reduces the twin thickness. Specifically, on a {111} plane, the partial dislocation slip needs to be "promoted" to the next {111} plane, so that twinning partials become available on successive planes one after another in a highly corrected fashion to thicken the twin. The "promotion-to-the-next-layer" probability is as follows [37]:

$$P_{\text{Partials}}^{\text{Promote}} = kdP_{\text{reaction}}^{\text{GB}} \quad , \tag{3}$$

where  $P_{\text{reaction}}^{\text{GB}}$  is the probability to accomplish the dislocation reaction and successfully promote identical partial slip on plane n + 1 at the GB site, *d* is the grain size and *k* is the scaling constant. From Eq. (3), one can notice that with grain size decreasing, the probability of twinning partial dislocations promotion to the next layer is decreasing. Therefore, after the nucleus of twins, it is difficult to emit twinning partial dislocations on the neighboring {111} plane, and this will lead to thinner twins. This result suggests that twinning in UFG/NC alloys with low SFE is operated via partial dislocations emission from the GBs, as indicated in Figs. 3(c) and 3(d).

Twin thickness has a significant impact on material properties [10, 11, 38] and applications [39]. Our results have experimentally illustrated the intrinsic relationship between grain size and twin thickness in UFG and NC materials. To optimize the mechanical properties of nanostructured materials, a physical model is urgently needed to describe the grain size effect on twin thickness in NC materials. Our results combined with the available knowledge of deformation twinning physics [14, 33, 40] provide some physical insight for the development of such model. Moreover, it is of great importance to understand the physical significance of the critical grain size below which twins could not exist, and this needs to be further investigated.

#### **Conclusions**

In summary, HPT and ECAP followed by cold rolling were used to achieve a wide range of grain sizes from  $\sim$ 5 to  $\sim$ 500 nm in a Cu–30% Zn alloy. The grain size effect on twin thickness in UFG and NC Cu–30% Zn alloys was investigated by HRTEM observations, and a systematic statistical analysis was made. It was found that twin thickness gradually reduces to one atomic layer (a stacking fault) with decreasing grain size down below  $\sim$ 20 nm. Stacking faults exist throughout the grain size range of  $\sim$ 5–500 nm, while twins only present in the grains with size larger than 20 nm. This shows a similar trend with that in the coarse-grained regime, although the twinning mechanisms are different. Importantly, our results provide statistical data for building a model to predict the twin thickness in UFG and NC fcc materials, which is helpful in designing metallic materials with good mechanical properties.

## **Experimental**

The material used in this study is a commercial Cu–30% Zn rod with a diameter of 10 mm. Its SFE is  $\sim$ 7 mJ/m<sup>2</sup>, which is much lower than that of Cu ( $\sim$ 41 mJ/m<sup>2</sup>) [41]. HPT processing and ECAP followed by cold rolling were used to process a series of samples with grain sizes in the NC regime (<100 nm) and UFG regime (100–1000 nm). In the case of HPT, disks with a diameter of  $\sim$ 10 mm and a thickness of  $\sim$ 0.8 mm were cut from the rod and processed for five rotations under an applied pressure of 6 GPa at room temperature (RT) and a rotation speed of 1 revolution per



minute, and the processing details can be found in Ref. 42. In the case of ECAP processing, the as-received rods were annealed at 600 °C for 1 h and then processed by ECAP at 220 °C for three passes using route Bc, in which the sample rod is rotated 90° after each pass, and detailed processing can be found in previous reports [43, 44]. To further reduce the grain size, the ECAP-processed Cu-30% Zn rods were subjected to RT rolling with thickness reductions of ~75% and ~95%, respectively. The rolling direction was along the longitudinal axis of the rod. For simplicity, these samples are labeled hereafter as HPT, ECAP + 75% rolling and ECAP + 95% rolling, respectively. Microstructural characterization was performed by TEM on an FEI Titan G<sup>2</sup> 60-300 (FEI, Hillsboro, OR, USA) operated at 300 kV. The thin foils for TEM observation were carefully prepared using the standard mechanical grinding and ion-milling on a Gatan PIPS 691 facility at a voltage of 4 kV.

# Acknowledgments

The authors acknowledge the financial support of the National Key R&D Program of China (2017YFA0204403), the National Natural Science Foundation of China (Grant Nos. 51741106, 51225102, and 2012CB932203), the Program for New Century Excellent Talents in University from Chinese Ministry of Education, the 8th "Liu Da Ren Cai Gao Feng" (B932203) from Jiangsu Province, China, the Fundamental Research Funds for the Central Universities (30919011256) and the Jiangsu Key Laboratory of Advanced Micro & Nano Materials and Technology. Transmission electron microscopy was performed in the Materials Characterization and Research Center of the Nanjing University of Science and Technology.

### References

- L. Lu, Y.F. Shen, X.H. Chen, L.H. Qian, and K. Lu: Ultrahigh strength and high electrical conductivity in copper. *Science* 304, 422 (2004).
- Y.F. Shen, L. Lu, Q.H. Lu, Z.H. Jin, and K. Lu: Tensile properties of copper with nano-scale twins. *Scripta Mater.* 52, 989 (2005).
- Y.T. Zhu, X.Z. Liao, and X.L. Wu: Deformation twinning in nanocrystalline materials. *Prog. Mater. Sci.* 57, 1 (2012).
- S. Ni, Y.B. Wang, X.Z. Liao, H.Q. Li, R.B. Figueiredo,
  S.P. Ringer, T.G. Langdon, and Y.T. Zhu: Effect of grain size on the competition between twinning and detwinning in nanocrystalline metals. *Phys. Rev. B* 84, 235401 (2011).
- Y.S. Li, N.R. Tao, and K. Lu: Microstructural evolution and nanostructure formation in copper during dynamic plastic deformation at cryogenic temperatures. *Acta Mater.* 56, 230 (2008).
- F. Zhao, L. Wang, D. Fan, B.X. Bie, X.M. Zhou, T. Suo, Y.L. Li, M.W. Chen, C.L. Liu, M.L. Qi, M.H. Zhu, and S.N. Luo:

Macrodeformation twins in single-crystal aluminum. *Phys. Rev. Lett.* **116**, 075501 (2016).

- M. Chen, E. Ma, K.J. Hemker, H. Sheng, Y. Wang, and X. Cheng: Deformation twinning in nanocrystalline aluminum. *Science* 300, 1275 (2003).
- **8.** X.Z. Liao, F. Zhou, E.J. Lavernia, D.W. He, and Y.T. Zhu: Deformation twins in nanocrystalline Al. *Appl. Phys. Lett.* **83**, 5062 (2003).
- X.L. Wu and Y.T. Zhu: Inverse grain-size effect on twinning in nanocrystalline Ni. *Phys. Rev. Lett.* 101, 025503 (2008).
- L. Lu, X. Chen, X. Huang, and K. Lu: Revealing the maximum strength in nanotwinned copper. *Science* 323, 607 (2009).
- Q. Huang, D. Yu, B. Xu, W. Hu, Y. Ma, Y. Wang, Z. Zhao,
  B. Wen, J. He, Z. Liu, and Y. Tian: Nanotwinned diamond with unprecedented hardness and stability. *Nature* 510, 250 (2014).
- X.H. An, S.D. Wu, Z.G. Wang, and Z.F. Zhang: Significance of stacking fault energy in bulk nanostructured materials: Insights from Cu and its binary alloys as model systems. *Prog. Mater. Sci.* 101, 1 (2019).
- Y.S. Li, Y. Zhang, N.R. Tao, and K. Lu: Effect of the Zener– Hollomon parameter on the microstructures and mechanical properties of Cu subjected to plastic deformation. *Acta Mater.* 57, 761 (2009).
- M.A. Meyers, O. Vöhringer, and V.A. Lubarda: The onset of twinning in metals: A constitutive description. *Acta Mater.* 49, 4025 (2001).
- S. Mahajan and G.Y. Chin: Formation of deformation twins in fcc crystals. *Acta Metall.* 21, 1353 (1973).
- Y.T. Zhu, X.Z. Liao, S.G. Srinivasan, Y.H. Zhao, M.I. Baskes,
  F. Zhou, and E.J. Lavernia: Nucleation and growth of deformation twins in nanocrystalline aluminum. *Appl. Phys. Lett.* 85, 5049 (2004).
- Y. Cao, Y.B. Wang, X.Z. Liao, M. Kawasaki, S.P. Ringer, T.G. Langdon, and Y.T. Zhu: Applied stress controls the production of nano-twins in coarse-grained metals. *Appl. Phys. Lett.* 101, 231903 (2012).
- R.J. McCabe, I.J. Beyerlein, J.S. Carpenter, and N.A. Mara: The critical role of grain orientation and applied stress in nanoscale twinning. *Nat. Commun.* 5, 3806 (2014).
- Y. Li, Y.H. Zhao, W. Liu, C. Xu, Z. Horita, X.Z. Liao, Y.T. Zhu, T.G. Langdon, and E.J. Lavernia: Influence of grain size on the density of deformation twins in Cu–30% Zn alloy. *Mater. Sci. Eng.*, A 527, 3942 (2010).
- I.J. Beyerlein, L. Capolungo, P.E. Marshall, R.J. McCabe, and C.N. Tomé: Statistical analyses of deformation twinning in magnesium. *Philos. Mag.* 90, 2161 (2010).
- V. Randle: Mechanism of twinning-induced grain boundary engineering in low stacking-fault energy materials. *Acta Mater.* 47, 4187 (1999).
- 22. S. Kibey, J.B. Liu, D.D. Johnson, and H. Sehitoglu: Predicting twinning stress in fcc metals: Linking twin-energy pathways to twin nucleation. *Acta Mater.* 55, 6843 (2007).



- 23. X.H. An, M. Song, Y. Huang, X.Z. Liao, S.P. Ringer, T.G. Langdon, and Y.T. Zhu: Twinning via the motion of incoherent twin boundaries nucleated at grain boundaries in a nanocrystalline Cu alloy. Scripta Mater. 72, 35 (2014).
- 24. J. Wang, N. Li, O. Anderoglu, X. Zhang, A. Misra, J.Y. Huang, and J.P. Hirth: Detwinning mechanisms for growth twins in facecentered cubic metals. Acta Mater. 58, 2262 (2010).
- 25. J.B. Cohen and J. Weertman: A dislocation model for twinning in fcc metals. Acta Metall. 11, 971 (1963).
- 26. J.A. Venables: Deformation twinning in face-centred cubic metals. Philos. Mag. 6, 379 (1961).
- 27. S. Mahajan: Critique of mechanisms of formation of deformation, annealing and growth twins: Face-centered cubic metals and alloys. Scripta Mater. 68, 95 (2013).
- 28. K.S. Kumar, H. Van Swygenhoven, and S. Suresh: Mechanical behavior of nanocrystalline metals and alloys. Acta Mater. 51, 5743 (2003).
- 29. Z. Shan, E.A. Stach, J.M.K. Wiezorek, J.A. Knapp, D.M. Follstaedt, and S.X. Mao: Grain boundary-mediated plasticity in nanocrystalline nickel. Science 305, 654 (2004).
- 30. V. Yamakov, D. Wolf, S.R. Phillpot, A.K. Mukherjee, and H. Gleiter: Dislocation processes in the deformation of nanocrystalline aluminium by molecular-dynamics simulation. Nat. Mater. 1, 45 (2002).
- 31. C.X. Huang, K. Wang, S.D. Wu, Z.F. Zhang, G.Y. Li, and S.X. Li: Deformation twinning in polycrystalline copper at room temperature and low strain rate. Acta Mater. 54, 655 (2006).
- 32. Y. Cao, S. Ni, X.Z. Liao, M. Song, and Y.T. Zhu: Structural evolutions of metallic materials processed by severe plastic deformation. Mater. Sci. Eng., R 133, 1 (2018).
- 33. V. Yamakov, D. Wolf, S.R. Phillpot, A.K. Mukherjee, and H. Gleiter: Deformation-mechanism map for nanocrystalline metals by molecular-dynamics simulation. Nat. Mater. 3, 43 (2004).

34. H. Van Swygenhoven, P.M. Derlet, and A.G. Froseth: Stacking fault energies and slip in nanocrystalline metals. Nat. Mater. 3, 399 (2004).

Article

- 35. S. Ni, Y.B. Wang, X.Z. Liao, R.B. Figueiredo, H.Q. Li, S.P. Ringer, T.G. Langdon, and Y.T. Zhu: The effect of dislocation density on the interactions between dislocations and twin boundaries in nanocrystalline materials. Acta Mater. 60, 3181 (2012).
- 36. N. Li, J. Wang, A. Misra, X. Zhang, J.Y. Huang, and J.P. Hirth: Twinning dislocation multiplication at a coherent twin boundary. Acta Mater. 59, 5989 (2011).
- 37. J.Y. Zhang, G. Liu, R.H. Wang, J. Sun, and E. Ma: Doubleinverse grain size dependence of deformation twinning in nanocrystalline Cu. Phys. Rev. B 81, 172104 (2010).
- 38. J.S. Li, Y. Cao, B. Gao, Y.S. Li, and Y.T. Zhu: Superior strength and ductility of 316L stainless steel with heterogeneous lamella structure. J. Mater. Sci. 53, 10442 (2018).
- 39. H.Y. Hsiao, C.M. Liu, H.W. Lin, T.C. Liu, C.L. Lu, Y.S. Huang, C. Chen, and K.N. Tu: Unidirectional growth of microbumps on (111)-oriented and nanotwinned copper. Science 336, 1007 (2012).
- 40. X.L. Ma, W.Z. Xu, H. Zhou, J.A. Moering, J. Narayan, and Y.T. Zhu: Alloying effect on grain-size dependent deformation twinning in nanocrystalline Cu-Zn alloys. Philos. Mag. 95, 301 (2015).
- 41. C.B. Carter and I.L.F. Ray: On the stacking-fault energies of copper alloys. Philos. Mag. 35, 189 (1977).
- 42. Y.H. Zhao, X.Z. Liao, Y.T. Zhu, Z. Horita, and T.G. Langdon: Influence of stacking fault energy on nanostructure formation under high pressure torsion. Mater. Sci. Eng., A 410, 188 (2005).
- 43. Y.T. Zhu and T.C. Lowe: Observations and issues on mechanisms of grain refinement during ECAP process. Mater. Sci. Eng., A 291, 46 (2000).
- 44. R.Z. Valiev and T.G. Langdon: Principles of equal-channel angular pressing as a processing tool for grain refinement. Prog. Mater. Sci. 51, 881 (2006).